

Problem 1. Find $\frac{dy}{dx}$.

(a) $y = x^3 + 3x^2 - 8x + 9;$

(b) $y = (x - 2)(x + 2)(x^2 + 4);$

(c) $y = \sin(x)\sqrt{x};$

(d) $y = \frac{1+x+x^2}{1+x^2+x^4};$

(e) $y = \tan^2(x^3).$

Problem 2 (Extra Credit). Find the maximum value of the function $f(x) = \sin x + \cos x$. Justify your answer.